## =IAdjoint

# Industrial Placement Presentation 

David Kurniadi Angdinata<br>MEng Mathematics and Computer Science 4

Friday, 04 October 2019

## Company profile

## Company profile



## Company profile



## Company profile



## Company profile

## Company profile



## Company profile

## Insight \& Control over your corporate accounts <br> Adjoint Treasury is a real-time payments and settlement platform for corporate treasury <br> 



Uplink: The distributed ledger for finance
Adjoint delivers enterprise applications for both finance professionals and technical adminstrators. We continually push the envelope to achieve excellence in security and privacy. Our technology is designed to support your ever-changing business needs.

## Organisation roles

## Organisation roles



## Organisation roles



## Organisation roles



## Organisation roles

## Organisation roles



## Adjoint

Adjoint builds financial workflow tools to simplify and control enterprise processes．
$\odot$ London，UK Bhttp：／／adjoint．io info＠adjoint．io Verified

## 园 Repositories 54 （T）Packages \＆People 6 III Projects

Pinned repositories

| fcl |
| :--- |
| A runtime for secure multiparty computation |
| Haskell $\$ 22$ |

## 园 bulletproofs

```
Bulletproofs are short non－interactive zero－
knowledge proofs that require no trusted setup
－Haskell \(422 \quad 821\)
```

```
pairing
Optimal ate pairing over Barreto-Naehrig curves
* Haskell $ % % 
```


## 国 sonic

Zero－Knowledge SNARKs from Linear－Size Universal and Updatable Structured Reference Strings

Haskell 24

```
uplink
A database for secure multiparty computation
- Haskell \ $ % 178 19
```

```
| elliptic-curve
Elliptic Curves
Haskell * & % %
```


## Cryptography roadmap

## Cryptography roadmap

## Cryptography roadmap

## GALOIS FIELDS

MACHINE OPTIMISATIONS

## Cryptography roadmap

## ELLIPTIC CURVES

GALOIS FIELDS

MACHINE OPTIMISATIONS

## Cryptography roadmap



## Cryptography roadmap



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## Cryptography roadmap

bulletproofs
SECP256K1 curve operations
SECP256K1 field arithmetic


## Cryptography roadmap

bulletproofs
SECP256K1 curve operations
SECP256K1 field arithmetic


An efficient library of Galois fields

## An efficient library of Galois fields

## galois-field: Galois field library

[ cryptography, library, mit ] [ Propose Tags ]
An efficient implementation of Galois fields used in cryptography research
[Skip to Readme]

## Modules

[Index] [Quick Jump]
Data
Field
Data.Field.Galois

## Versions [faq]

0.1.0, 0.2.0, 0.2.1, 0.3.0, 0.4.0, 0.4.1, 1.0.0

## Change log

ChangeLog.md

## Dependencies

base (>=4.10 \& \& <5), groups, integer-gmp, MonadRandom, poly $\left(>=0.3 .2\right.$ ), protolude ( $==0.2 .^{*}$ ), semirings $(>=0.5$ ),
tasty-quickcheck, vector, wl-pprint-text [details]

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## An efficient library of Galois fields

## galois-field: Galois field library

[ cryptography, Library, mit ] [ Propose Tags ]

An efficient implementation of Galois fields used in cryptography research [Skip to Readme]

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- Prime fields and extension fields


## An efficient library of Galois fields



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galois-field: Galois field library
[ cryptography, library, mit ] [ Propose Tags ]
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[Skip to Readme]
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- Prime fields and extension fields
- Extensive usage of type system
- Slow performance of binary fields


## An efficient library of Galois fields

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galois-field: Galois field library
[ cryptography, library, mit ] [ Propose Tags ]
An efficient implementation of Galois fields used in cryptography research
[Skip to Readme]
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[Index] [Quick Jump]
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tasty-quickcheck, vector, wi-pprint-text [details]
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```
- Prime fields and extension fields
- Extensive usage of type system
- Slow performance of binary fields
- Square roots and scalar multiplication
```


## An efficient library of Galois fields

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galois-field: Galois field library
[ cryptography, library,mit ] [ Propose Tags ]
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[Skip to Readme]
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[Index] [Quick Jump]
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```
- Prime fields and extension fields
- Extensive usage of type system
- Slow performance of binary fields
- Square roots and scalar multiplication
- Heavy compile-time and run-time optimisations
```


## An efficient library of Galois fields



## An efficient library of Galois fields



## An efficient library of Galois fields



## A universal library of elliptic curves

## A universal library of elliptic curves

## elliptic-curve: Elliptic curve library

## [ cryptography, library, mit ] [ Propose Tags ]

An extensible library of elliptic curves used in cryptography research
[Skip to Readme]

## Modules

[Index] [Ouick Jump]
Data
Data.Curve
Data.Curve.Binary
Data.Curve.Binary.SECT113R1
Data.Curve.Binary.SECT113R2 Data.Curve.Binary.SECT131R1 Data.Curve.Binary.SECT131R2 Data.Curve.Binary.SECT163K1 Data.Curve.Binary.SECT163R1

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Category
Cryptography

## A universal library of elliptic curves

elliptic-curve: Elliptic curve library
[ cryptography, library, mit ] [ Propose Tags ]

An extensible library of elliptic curves used in cryptography research
[Skip to Readme]

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Category
Cryptography

- Eighty elliptic curve domain parameters


## A universal library of elliptic curves

elliptic-curve: Elliptic curve library
[ cryptography, library, mit ] [ Propose Tags ]

An extensible library of elliptic curves used in cryptography research
[Skip to Readme]
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[Index] [Ouick Jump]
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Data.Curve.Binary.SECT113R2
Data.Curve.Binary.SECT131R1
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Cryptography

- Eighty elliptic curve domain parameters
- Elliptic curve multi-parameter type class


## A universal library of elliptic curves

elliptic-curve: Elliptic curve library
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An extensible library of elliptic curves used in cryptography research
[Skip to Readme]

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[Index] [Ouick Jump]
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Category
Cryptography
```

- Eighty elliptic curve domain parameters
- Elliptic curve multi-parameter type class
- Elliptic curve point associated type


## A universal library of elliptic curves

elliptic-curve: Elliptic curve library
[ cryptography, library, mit ] [ Propose Tags ]
An extensible library of elliptic curves used in cryptography research
[Skip to Readme]

Modules
[Index] [Ouick Jump]
Data
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Data.Curve.Binary.SECT113R2
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Adjoint Inc (info@adjoint.io)
Category
Cryptography
```

- Eighty elliptic curve domain parameters
- Elliptic curve multi-parameter type class
- Elliptic curve point associated type
- Elliptic curve point addition formulas


## A universal library of elliptic curves

elliptic-curve: Elliptic curve library
[ cryptography, library, mit ] [ Propose Tags ]

An extensible library of elliptic curves used in cryptography research
[Skip to Readme]

Modules
[Index] [Ouick Jump]
Data
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Cryptography

- Eighty elliptic curve domain parameters
- Elliptic curve multi-parameter type class
- Elliptic curve point associated type
- Elliptic curve point addition formulas
- Elliptic curve source code generator


## A universal library of elliptic curves



## A universal library of elliptic curves



## A universal library of elliptic curves



A polymorphic library of bilinear pairings

## A polymorphic library of bilinear pairings

## pairing: Bilinear pairings

[ cryptography, library, mit ] [ Propose Tags ]
Optimal Ate pairing over Barreto-Naehrig curves
[Skip to Readme]
Versions [faq]
$0.1 .0,0.1 .1,0.1 .2,0.1 .3,0.1 .4,0.2,0.3 .0,0.3 .1,0.4 .1,0.4 .2,0.5 .0$, 1.0.0

## Modules

[Index] [Quick Jump]
Data
Data.Pairing
Data.Pairing.Ate
Data.Pairing.BLS12381
Data.Pairing.BN254

## Change log

ChangeLog.md

## Dependencies

base ( $>=4.10 \& \&<5$ ), bytestring, elliptic-curve ( $==0.3 .^{\prime}$ ), errors, galois-field (==1.'), groups, MonadRandom, protolude ( $=0.2$. $^{\prime}$ ), tasty-quickcheck [details]

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## A polymorphic library of bilinear pairings

## pairing: Bilinear pairings

[ cryptography, Library, mit ] [ Propose Tags ]

Optimal Ate pairing over Barreto-Naehrig curves
[Skip to Readme]

## Modules

[Index] [Quick Jump]
Data
Data.Pairing
Data.Pairing.Ate
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```
Versions [faq]
    0.1.0,0.1.1, 0.1.2,0.1.3,0.1.4,0.2,0.3.0,0.3.1,0.4.1, 0.4.2, 0.5.0,
    1.0.0
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## Change log

```
ChangeLog.md
```


## Dependencies

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```


## License

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```

- Pairing for BN and BLS


## A polymorphic library of bilinear pairings

## pairing: Bilinear pairings

[ cryptography, library, mit ] [ Propose Tags ]

Optimal Ate pairing over Barreto-Naehrig curves
[Skip to Readme]

## Modules

[Index] [Quick Jump]
Data
Data.Pairing
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Data.Pairing.BN254

```
Versions [faq]
    0.1.0, 0.1.1,0.1.2,0.1.3, 0.1.4, 0.2,0.3.0,0.3.1,0.4.1, 0.4.2,0.5.0,
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```


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- Pairing for BN and BLS
- General bilinear pairing type class


## A polymorphic library of bilinear pairings

## pairing: Bilinear pairings

[ cryptography, library, mit ] [ Propose Tags ]

Optimal Ate pairing over Barreto-Naehrig curves
[Skip to Readme]

## Modules

[Index] [Quick Jump]
Data
Data.Pairing
Data.Pairing.Ate
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- Pairing for BN and BLS
- General bilinear pairing type class
- General optimal ate pairing algorithm


## A polymorphic library of bilinear pairings

## pairing: Bilinear pairings

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Optimal Ate pairing over Barreto-Naehrig curves
[Skip to Readme]

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[Index] [Quick Jump]
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- Pairing for BN and BLS
- General bilinear pairing type class
- General optimal ate pairing algorithm
- Seven elliptic curve bilinear pairings


## A polymorphic library of bilinear pairings

## pairing: Bilinear pairings

[ cryptography, Library, mit ] [ Propose Tags ]

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[Skip to Readme]
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[Index] [Quick Jump]
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- Pairing for BN and BLS
- General bilinear pairing type class
- General optimal ate pairing algorithm
- Seven elliptic curve bilinear pairings
- BN elliptic curve hashing function


## A polymorphic library of bilinear pairings



## A polymorphic library of bilinear pairings



## Conclusion

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Powerful type system in Haskell

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Crucial performance optimisations in Haskell

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Mathematical background behind zero-knowledge proofs

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Mathematical background behind zero-knowledge proofs

Cryptographic applications of number theory

## Conclusion

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Mathematical background behind zero-knowledge proofs

Cryptographic applications of number theory

Collaborative communication and productivity management

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